# M.Sc. MATHEMATICS

# LOCF SYLLABUS 2023



Department of Mathematics
School of Computing Sciences
St. Joseph's College (Autonomous)
Tiruchirappalli - 620 002, Tamil Nadu, India

#### Vision

Forming globally competent, committed, compassionate and holistic persons, to be men and women for others, promoting a just society.

#### Mission

- Fostering learning environment to students of diverse background, developing their inherent skills and competencies through reflection, creation of knowledge and service.
- Nurturing comprehensive learning and best practices through innovative and value-driven pedagogy.
- Contributing significantly to Higher Education through Teaching, Learning, Research and Extension.

### **Programme Educational Objectives (PEOs)**

- Graduates will be able to accomplish professional standards in the global environment.
- Graduates will be able to uphold integrity and human values.
- Graduates will be able to appreciate and promote pluralism and multiculturalism in working environment

#### **Programme Outcomes (POs)**

- 1. Graduates will be able to apply assimilated knowledge to evolve tangible solution to emerging problems.
- 2. Graduates will be able to analyze and interpret data to create and design new knowledge.
- 3. Graduates will be able to engage in innovative and socially relevant research and effectively communicate the findings.
- 4. Graduates will become ethically committed professional and entrepreneurs upholding human values.
- 5. Graduates imbibed with ethical values and social concern will be able to understand and appreciate cultural diversity, social harmony and ensure sustainable environment.

#### **Programme Specific Objectives (PSOs)**

#### Graduate will be able to

- 1. Appreciate the emphasis given on teaching the fundamentals, the basic concepts, definitions with a variety of examples.
- 2. Realise the importance given to applications by applying the concepts studied for designing models to solve real life problems.
- 3. Develop the skill to solve problems which appear in the various examinations based on the concepts learned which in turn will hone the problem solving skills of students and help them to pass competitive examinations including CSIR-NET, SET, IAS, etc
- 4. Learn application oriented subjects which will impress upon them their responsibility to the society.
- 5. Get proper orientation that a research degree is not end of learning. They are encouraged to publish papers on a continual basis in the standard journals during and after Ph.D.

# **CONTINUOUS INTERNAL ASSESSMENT Categorizing Outcome Assessment Levels Using Bloom's Taxonomy**

Level	Cognitive Domain	Description
K1	Remember	It is the ability to remember the previously learned concepts or ideas.
K2	Understand	The learner explains concepts or ideas.
К3	Apply	The learner uses existing knowledge in new contexts.
K4	Analyse	The learner is expected to draw relations among ideas and to compare and contrast.
K5	Evaluate	The learner makes judgements based on sound analysis.
K6	Create	The learner creates something unique or original.

### **Question Paper Blueprint for Mid and End Semester Tests**

Duration: 2	2 Hours				Maximum Marks: 60					
	Section		K level*							
	K1	K2	К3	K4	K5	K6	Marks			
A (no choice)		7						$7 \times 1 = 7$		
B (no choice)			5					$5 \times 3 = 15$		
C (either or	type)			3				$3 \times 6 = 18$		
	Courses with K4 as the highest cognitive level				2					
	Courses with K5 as the highest cognitive level wherein one question each on K4 and K5 is compulsory. (Note:K4 has two questions whereas, K5 has no choice.)				1	1				
<b>D</b> (2 out of 3)					Mid	Sem		$2 \times 10 = 20$		
	Courses with K6 as the highest cognitive level wherein one question each on K5 and					End	Sem			
	K6 is compulsory. (Note: <b>Mid Sem:</b> K4 has two questions whereas, K5 has no choice; <b>End sem:</b> K5 has two questions whereas, K6 has no choice)				1	1	1			
				-		-	Total	60		

<sup>\*</sup> K4 and K5 levels will be assessed in the Mid semester test whereas K5 and K6 levels will be assessed in the End semester test.

### **Question Paper Blueprint for Mid and End Semester Tests** (For quantitative courses only)

Duration: 2 Hours Maximu									
S. A. S.									
Section	K1	K2	КЗ	K4	K5	К6	Marks		
A (no choice)	5	4					9 × 1 = 9		
B (either or type)			2	1			$3\times 5=15$		
C (2 out of 3)					1	1*	2 × 18 = 36		
					•	Total	60		

**NOTE:** K4 and K5 will be assessed in the Mid semester test whereas K5 and K6 will be assessed in the End semester test.

# SEMESTER EXAMINATION **Question Paper Blueprint for Semester Examination**

Duration: 3	Maximum Marks: 100							
	G			K le	evel			3.6 3
	Section		K2	К3	K4	K5	K6	Marks
A (no choice,	two questions from each unit)	10						$10 \times 1 = 10$
B (no choice,	two questions from each unit)		10					$10 \times 3 = 30$
C (either or	C (either or type, one question from each unit)			5				$5 \times 6 = 30$
	Courses with K4 as the highest cognitive level				3			
D (3 out of 5, one question from each	Courses with K5 as the highest cognitive level wherein two K4 questions and one K5 question are compulsory. (Note: Three questions on K4 and two questions on K5)				2	1		3 × 10 = 30
unit)	Courses with K6 as the highest cognitive level wherein one question each on K4, K5, and K6 is compulsory. (Note: Two questions each on K4 and K5 and one question on K6)				1	1	1	
			-		-	-	Total	100

<sup>\*</sup> K6 compulsory

# **Question Paper Blueprint for Semester Examination** (For quantitative courses only)

Section	Marks	K level						
A	$10 \times 1 = 10$	K1						
В	$5 \times 6 = 30$ (eitheror)	K2 (Q. No. 11 & 12) K3 (Q. No. 13, 14 & 15)						
С	4 × 15 = 60 (4 out of 5)	K4 (Q. No. 16 & 17) K5 (Q. No. 18 & 19) K6 (Q. No. 20 compulsory)						
Total Marks: 100								

### **Evaluation Pattern for Part IV One/Two Credit Courses**

Title of the Course	CIA	Semester Examination	Total Marks
Internship	100		100
UG Skill Enhancement Course (Non Major Elective) Foundation Course PG Ability Enhancement Course	20 + 10 + 20 = 50	50 (External member from the Department)	100
Value Education	50	50 (CoE)	100

		M.Sc. MATHEMATICS PROGRAMME PATTERN						
		Course Details			Sche	me of	Exams	
Sem	Course Code	Title of the Course	Hours	Credits	CIA	SE	Final	
2011	23PMA1CC01	Core Course - 1: Algebraic Structures	6	6	100	100	100	
	23PMA1CC02	Core Course - 2: Real Analysis - 1	6	6	100	100	100	
	23PMA1CC03	Core Course - 3: Ordinary Differential Equations	6	4	100	100	100	
1	23PMA1ES01	Elective - 1: Graph Theory and its Applications	5	3	100	100	100	
1	23PMA1ES02	Elective - 2: Fuzzy Sets and Their Applications	5	3	100	100	100	
	23PMA1AE01	Ability Enhancement Course: Problem Solving in Advanced Mathematics	2	1	100	-	100	
		Total	30	23				
	23PMA2CC04	Core Course - 4: Advanced Algebra	6	6	100	100	100	
]	23PMA2CC05	Core Course - 5: Real Analysis - 2	5	4	100	100	100	
	23PMA2CC06	Core Course - 6: Complex Analysis	6	5	100	100	100	
	23PMA2SP01	Self- paced Learning: History of Mathematics*	-	2	50	50	50	
2	23PMA2ES03A	Elective - 3: Algebraic Number Theory	5	1	100	100	100	
	23PMA2ES03B	PMA2ES03B Elective - 3: Optimization Techniques						
[	23PSS2SE01	Skill Enhancement Course: Soft Skills	4	3	100	-	100	
	23PMA2EG01A	Generic Elective - 1 (WS): Mathematical Foundations for Computer Applications	4 3		100	100	100	
	23PMA2EG01B	Conorio Flortivo 1 (WS): Mathematical Foundations for						
[	-	Extra Credit Courses (MOOC/Certificate Courses) - 1	-	(3)				
		Total	30	27(3)				
	23PMA3CC07	Core Course - 7: Measure and Integration	6	6	100	100	100	
	23PMA3CC08	Core Course - 8: Topology	6	6	100	100	100	
]	23PMA3CC09	Core Course - 9: Classical Dynamics	5	5	100	100	100	
3	23PMA3CC10	Core Course - 10: Stochastic Processes	4	4	100	100	100	
3	23SCS3CC01	Common Core: Design and Analysis of Algorithms	5	4	100	100	100	
	23PMA3EG02	Generic Elective - 2 (BS): Operations Research	4	3	100	100	100	
İ	_	Extra Credit Courses (MOOC/Certificate Courses) - 2	-	(3)				
<u> </u>		Total	30	28(3)				
	23PMA4CC11	Core Course - 11: Functional Analysis	6	6	100	100	100	
	23PMA4CC12	Core Course - 12: Calculus of Variations and Integral Equations	6	6	100	100	100	
1	23PMA4CC13	Core Course - 13: Partial Differential Equations	5	5	100	100	100	
4	23PMA4ES04A	Elective - 4: Automata Theory						
1	23PMA4ES04B	Elective - 4: Differential Geometry	5	4	100	100	100	
[	23PMA4PW01	Project Work and Viva Voce	8	5	100	100	100	
[	23PMA4CE01	Comprehensive Examination*	-	2	50	50	50	
	-	Extra Credit Courses (MOOC/Certificate Courses) - 3	-	(3)				
		Total	30	28(3)				
2 - 4	23PCW4OR01	Outreach Programme (SHEPHERD)	-	4				
1 - 4		Total (2years)	120	110				

<sup>\*-</sup> for grade calculation 50 marks are converted into 100 in the mark statements

Semester	Course code	Title of the Course	Hours/Week	Credits
1	23PMA1CC01	Core Course - 1: Algebraic Structures	6	5

To gain a deep understanding of important concepts of class equations and Sylow's theorem in group theory and develop proficiency in their applications

To investigate the structure and behavior of algebraic systems and classify them based on certain properties, and apply the concepts to solve various mathematical problems in diverse area of studies

To understand the concepts of linear transformations and their properties, simplifying their representation, and analyzing their behaviors in various mathematical contexts

To simplify matrix representations while the rational canonical form aims to classify matrices, study minimal polynomials, and compute matrix powers efficiently

To provide insights into Eigen values and quadratic forms

UNIT I (18 Hours)

Counting Principle - Class equation for finite groups and its applications - Sylow's theorems (For theorem 2.12.1, First proof only).

UNIT II (18 Hours)

Solvable groups - Direct products - Finite abelian groups- Modules.

UNIT III (18 Hours)

Linear Transformations: Canonical forms – Triangular form - Nilpotent transformations.

UNIT IV (18 Hours)

Jordan form - rational canonical form.

UNIT V (18 Hours)

Trace and transpose - Hermitian, unitary, normal transformations, real quadratic form.

Teaching Methodology	Chalk and talk, Lectures, Demonstrations, PPT.
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#### **Books for Study**

1. Herstein, I. N. (1975). *Topics in Algebra* (2<sup>nd</sup> ed.). Wiley Eastern Limited.

Unit I: Chapter 2: Sections 2.11 and 2.12 (Omit Lemma 2.12.5)

Unit II: Chapter 5: Section 5.7 (Lemma 5.7.1, Lemma 5.7.2, Theorem 5.7.1)

Chapter 2: Section 2.13 and 2.14 (Theorem 2.14.1 only)

Chapter 4: Section 4.5

**Unit III:** Chapter 6: Sections 6.4, 6.5

**Unit IV:** Chapter 6: Sections 6.6 and 6.7

**Unit V:** Chapter 6: Sections 6.8, 6.10 and 6.11 (Omit 6.9)

#### **Books for Reference**

1. Artin, M. (1991). Algebra. Prentice Hall.

2. Bhattacharya, P. B., Jain, S. K. & Nagpaul, S. R. (1997). *Basic abstract algebra* (2<sup>nd</sup> ed.). Cambridge University Press (Indian Edition).

- 3. Luther, I. S. & Passi, I. B. S. (1999). *Algebra, vol. I—Groups (1996); Vol. II Rings*. Narosa Publishing House.
- 4. Malik, D. S., Mordeson, J. N. & Sen, M. K. (1997). *Fundamental of abstract algebra* (International Edition). McGraw Hill.
- 5. Jacobson, N. & Freeman, W. H. (1980). *Basic algebra, Vol. I & II.* Hindustan Publishing Company.

#### **Web Sources**

- 1. http://mathforum.org, http://ocw.mit.edu/ocwweb/Mathematics,
- 2. http://www.opensource.org, www.algebra.com

	Course Outcomes	
CO No.	CO-Statements On successful completion of this course, students will be able to	Cognitive Levels (K - Level)
CO1	recall basic counting principle, define class equations to solve problems, explain Sylow's theorems and apply the theorem to find number of Sylow subgroups.	K1
CO2	define Solvable groups, define direct products, examine the properties of finite abelian groups, define modules	K2
CO3	define similar Transformations, define invariant subspace, explore the properties of triangular matrix, to find the index of nilpotence to decompose a space into invariant subspaces, to find invariants of linear transformation, to explore the properties of nilpotent transformation relating nilpotence with invariants.	К3
CO4	define Jordan, canonical form, Jordan blocks, define rational canonical form, define companion matrix of polynomial, find the elementary devices of transformation, apply the concepts to find characteristic polynomial of linear transformation.	K4
CO5	define trace, define transpose of a matrix, explain the properties of trace and transpose, to find trace, to find transpose of matrix, to prove Jacobson lemma using the triangular form, define symmetric matrix, skew symmetric matrix, adjoint, to define Hermitian, unitary, normal transformations and to verify whether the transformation in Hermitian, unitary and normal	K5
CO6	interpret and evaluate ideas of theory of Eigen values and quadratic forms.	K6

				]	Relation	nship N	<b>Iatrix</b>				
Semester	Cours	se code			Title o	f the Co	urse			Hours	Credits
1	23PMA	1CC01		Core	Course -	1: Algebra	aic Struct	ures		6	5
Course Outcomes	Pro	Programme Outcomes (POs)  Programme Specific Outcomes (PSOs)				Chitcomes (PUS)					
	PO1	PO2	PO3	PO4	PO5	PSO 1	PSO 2	PSO3	PS O 4	PSO5	COs
CO1	3	3	3	2	1	3	2	3	2	3	2.5
CO2	2	3	3	2	2	2	3	2	1	3	2.3
CO3	3	2	3	2	2	3	2	2	2	2	2.3
CO4	3	3	2	2	2	3	3	3	2	3	2.6
CO5	2	3	3	2	1	3	3	2	2	3	2.4
CO6	2	3	3	2	1	3	3	2	2	3	2.4
Mean overall Score								2.42 (High)			

Semeste r	Course Code	Title of the Course	Hours/ Week	Credit s
1	23PMA1CC0 2	Core Course - 2: Real Analysis -1	6	5

To enable the students to learn the basic concepts of real analysis

To understand proof techniques in analysis and be well prepared for the advanced courses like functional analysis and advanced analysis

To work comfortably with functions of bounded variation, Riemann – Stieltjes Integration

To work with Convergence of infinite series and infinite product

To know uniform convergence and its interplay between various limiting operations

UNIT I (18 Hours)

Introduction – Properties of monotonic functions – Functions of bounded variation – Total variation – Additive property of total variation – Total variation on [a, x] as a function of x – Functions of bounded variation expressed as the difference of two increasing functions – Continuous functions of bounded variation – Absolute and conditional convergence – Dirichlet's test and Abel's test – Rearrangement of series – Riemann's theorem on conditionally convergent series.

UNIT II (18 Hours)

Introduction – Notation – The definition of the Riemann – Stieltjes integral – Linear Properties – Integration by parts– Change of variable in a Riemann – Stieltjes integral – Reduction to a Riemann Integral – Euler's summation formula – Monotonically increasing integrators, Upper and lower integrals – Additive and linearity properties of upper, lower integrals – Riemann's condition – Comparison theorems.

UNIT III (18 Hours)

Integrators of bounded variation—Sufficient conditions for the existence of Riemann—Stieltjes integrals—Necessary conditions for the existence of RS integrals—Mean value theorems—integrals as a function of the interval—Second fundamental theorem of integral calculus—Change of variable—Second Mean Value Theorem for Riemann integral—Riemann—Stieltjes integrals depending on a parameter—Differentiation under integral sign—Lebesgue criteriaon for existence of Riemann integrals.

UNIT IV (18 Hours)

Double sequences – Double series – Rearrangement theorem for double series – A sufficient condition for equality of iterated series – Multiplication of series – Cesaro summability – Infinite products – Multiplication of power series – The Taylor's series generated by a function – Bernstein's theorem – Abel's limit theorem – Tauber's theorem

UNIT V (18 Hours)

Pointwise convergence of sequences of functions – Examples of sequences of real – valued functions – Uniform convergence and continuity – Cauchy condition for uniform convergence – Uniform convergence of infinite series of functions – Riemann – Stieltjes integration – Non–uniform Convergence and Term–by–term Integration – Uniform convergence and differentiation – Sufficient condition for uniform convergence of a series – Mean convergence.

#### **Books for Study:**

1. Apostol, T. M. (1974). *Mathematical analysis* (2<sup>nd</sup> ed.). Addison-Wesley Publishing Company Inc.

**Unit – I** Chapter 6(Sec 6.1 – 6.8) and Chapter 8 (8.8, 8.15, 8.17, 8.18)

**Unit – II** *Chapter 7 (Sec 7.1 – 7.14)* 

**Unit – III** *Chapter 7(Sec 7.15 – 7.26)* 

**Unit – IV** Chapter 8(Sec 8.20 – 8.26) and Chapter 9 (9.14 9.15, 9.19, 9.20, 9.22, 9.23)

**Unit – V** Chapter -9 (Sec 9.1 to 9.6, 9.8,9.9,9.10,9.11, 9.13)

- 1. Bartle, R. G. (1976). Real analysis. John Wiley & Sons Inc.
- 2. Rudin, W. (1976). *Principles of mathematical analysis* (3<sup>rd</sup> ed.). McGraw Hill Company.
- 3. Malik, S. C. & Arora, S. (1991). Mathematical analysis. Wiley Eastern Limited.
- 4. Arora, S. & Lal, B. (1991). *Introduction to real analysis*. Satya Prakashan.
- 5. Gelbaum, B. R. & Olmsted, J. (1964). Counter examples in analysis. Holden day.
- 6. Gupta, A. L. & Gupta, N. R. (2003). *Principles of real analysis*. Pearson Education (Indian print).

	Course Outcomes						
CO No.	0						
CO1	acquire knowledge of functions of bounded variation, Riemann-Stieltjes, and uniform convergence	K1					
CO2	understand the concepts of Riemann- Stieltjes integral, uniform convergence and its properties.	K2					
CO3	apply the properties of bounded variation, Riemann integral in convergence of sequence of functions.	К3					
CO4	evaluate the properties of convergence of series and Riemann integrablity of functions	K4					
CO5	analyze the functions of bounded variation, Riemann integral and double series.	K5					
CO6	construct proofs and examples of Riemann- Stieltjes integration, convergence of sequence of functions and double series	К6					

					Relatio	nship	Matrix	X			
Semester	Course code Title of the Cou						ourse			Hours	Credits
1	23PMA	1CC02		Co	re Cours	e - 2: Rea	l Analys	is -1		6	5
Course Outcomes	F	rogramn	ne Outco	mes (PO	s)	Progr	amme S	pecific O	utcomes (	(PSOs)	Mean Score of
o accomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO 2	PSO3	PSO4	PSO5	COs
CO1	2	3	3	3	2	3	3	3	3	2	2.7
CO2	3	2	3	3	2	2	3	2	3	3	2.6
CO3	3	3	3	2	3	3	3	2	3	3	2.8
CO4	3	2	3	3	2	3	2	3	3	3	2.7
CO5	3	3	3	2	3	3	3	3	3	3	2.9
CO6	3	3	3	3	2	2	3	2	2	3	2.6
	•	•	•	•	•	•		М	ean over	all Score	2.7 (High)

Semester	Course code	Title of the Course	Hours	Credits
1	23PMA1CC 03	Core Course - 3: Ordinary Differential Equations	6	4

Develop strong background on finding solutions to linear differential equations with constant and variable coefficients and also with singular points

Understanding the concepts of Linear dependence and independence, Wronskian, Singular points, Bessel function, Lipschitz condition, etc.,

Develop strong background on finding solutions to Legendre equation, Euler equation, Exact equation and its applications

Give a depth knowledge of solving initial value problems in ordinary differential equations

Skill to study the existence and uniqueness of solution in first and higher order differential equations

#### **UNIT I: Linear Equations with Constant Coefficients**

(18 Hours)

Second order homogeneous equations-Initial value problems-Linear dependence and independence-Wronskian and a formula for Wronskian-Non-homogeneous equation of order two. **Chapter 2: Sections 1 to 6** 

#### **UNIT II: Linear Equations with Constant Coefficients**

(18 Hours)

Homogeneous and non-homogeneous equation of order n —Initial value problems-Annihilator method to solve non-homogeneous equation - Algebra of constant coefficient operators. **Chapter 2: Sections 7 to 12** 

#### **UNIT III: Linear Equation with Variable Coefficients**

(18 Hours)

Initial value problems -Existence and uniqueness theorems – Solutions to solve a non-homogeneous equation – Wronskian and linear dependence – reduction of the order of a homogeneous equation – homogeneous equation with analytic coefficients-The Legendre equation. Chapter: 3 Sections 1 to 8 (Omit section 9)

#### **UNIT IV: Linear Equation with Regular Singular Points**

**(18 Hours)** 

Euler equation – Second order equations with regular singular points –Exceptional cases – Bessel Function. Chapter 4: Sections 1 to 4 and 6 to 8 (Omit sections 5 and 9)

UNIT V (18 Hours)

Existence and uniqueness of solutions to first order equations: Equation with variable separated – Exact equation – method of successive approximations – the Lipschitz condition – convergence of the successive approximations and the existence theorem.

#### Chapter 5: Sections 1 to 6 (Omit Sections 7 to 9)

Teaching Methodology	Chalk and talk, Lectures, Demonstrations, PPT.
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#### **Books for Study**

1. Coddington, E. A. (1987). *An introduction to ordinary differential equations* (3<sup>rd</sup> ed.). Prentice-Hall of India.

#### **Books for Reference**

- 2. Boyce, W. E. & Prima, R. C. D (1967). *Elementary differential equations and boundary value problems*. John Wiley & Sons, New York.
- 3. Simmons, G. F. (1974). *Differential equations with applications and historical notes*. Tata McGraw Hill, New Delhi.
- 4. Lebedev, N. N. (1965). *Special functions and their applications*. Prentice Hall of India, New Delhi.
- 5. Reid, W.T. (1971). Ordinary differential equations. John Wiley & Sons, New York.
- 6. Raisinghania, M. D. (2001). *Advanced differential equations*. S. Chand & Company Ltd, New Delhi.
- 7. Rai, B., Choudary, D. P. & Freedman, H. I. (2002). *A course in ordinary differential equations*. Narosa Publishing House, New Delhi.

#### **Web Source**

- 1. http://mathforum.org, http://ocw.mit.edu/ocwweb/Mathematics,
- 2. http://www.opensource.org, www.mathpages.com

	Course Outcomes					
CO	CO-Statements	Cognitive Levels				
No.	On successful completion of this course, students will be able to	(K - Level)				
CO1	establish the qualitative behaviour of solutions of systems of differential equations	K1				
CO2	recognize the physical phenomena modelled by differential equations and dynamical systems.	K2				
CO3	analyse solutions using appropriate methods and give examples	K3				
CO4	formulate Wronskian for initial value problems	K4				
CO5	understand and use various theoretical ideas and results that underlie the mathematics in this course.	K5				
CO6	formulate and solve the different kinds of ordinary differential equations.	K6				

					Relatio	onship l	Matrix				
Semester	emester Course code Title of the Course				Hours	Credits					
1	23PM	A1CC03	Core Course - 3: Ordinary Differential Equations					6	4		
Course Outcomes	Programme Outcomes (POs)				)	Prog	ramme S	pecific Ou	itcomes (l	PSOs)	Mean Score of COs
	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	
CO1	3	3	2	3	3	3	3	3	2	3	2.8
CO2	2	2	2	3	3	3	3	3	2	3	2.6
CO3	2	2	3	3	3	3	3	3	3	3	2.8
CO4	3	3	2	3	3	3	3	3	2	3	2.8
CO5	2	2	3	2	3	2	3	3	2	3	2.5
CO6	2	2	3	3	3	3	3	3	3	3	2.8
Mean overall Score						2.7 (High)					

Semester	Course code	Title of the Course	Hours\Week	Credits
1	23PMA1ES01	Elective - 1: Graph Theory	5	3
		and its Applications		

To introduce the basic concepts of graphs and digraphs

To introduce the notion of connectivity in graphs and the concept of trees

To familiarize on the ideas of independent sets, coverings, matchings and factors

To acquaint on Eulerian, Hamiltonian and planar graphs and the concept of graph colorings, and the notion of duality in graphs

To develop the skill of formulating real life problems to graphical models and finding solutions

UNIT I (15 Hours)

Basic concepts – Subgraphs – Degrees of vertices – Paths and connectedness – Operations on graphs - Directed graphs: Basic concepts.

UNIT II (15 Hours)

Vertex cuts and Edge cuts – Connectivity and Edge – Connectivity – Trees: Definition, Characterization and Simple Properties – Applications: Prim's Algorithm.

UNIT III (15 Hours)

Vertex Independent sets and Vertex Coverings – Edge Independent sets – Matching's and Factors – Eulerian graphs – Hamiltonian graphs.

UNIT IV (15 Hours)

Vertex colorings - Applications of Graph Coloring - Critical graphs - Edge colorings of graphs.

UNIT V (15 Hours)

Planar and nonplanar graphs – Euler formula and its consequences –  $K_5$  and  $K_{3,3}$  are nonplanar Graphs – Dual of a plane Graph - The Four–Color theorem and the Heawood Five–Color theorem.

**Note:** Theorems, propositions and results which are starred in the book are to be omitted.

Teaching Methodology	Chalk and Talk and PPT
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#### **Books for Study**

1. Balakrishnan, R. & Ranganathan, K. (2000). *A Textbook of graph theory*. Springer (India) Private Limited.

**Unit I:** *Chapter I:* 1.1 - 1.4, 1.7, *Chapter II:* 2.1,

Unit II: Chapter III: 3.1, 3.2, Chapter IV: 4.1, Chapter X: 10.3

**Unit III:** Chapter V: 5.1 to 5.3, Chapter VI: 6.1, 6.2

Unit IV: Chapter VII: 7.1, 7.2 and 7.4

Unit V: Chapter VIII: 8.1 to 8.5

#### **Books for Reference**

1. Bondy, J. A. & Murty, U. S. R. (1976). *Graph theory with applications*. Macmillan Press Ltd.

- 2. Harary, F. (1969). *Graph theory*. Addison Wesley Publishing Company Inc.
- 3. Chartrand, G., Lesniak, L. & Zhang, P. (2010). Graphs and digraphs. CRC press.

#### **Web Sources**

- 1. https://onlinecourses.nptel.ac.in/noc20\_ma05/preview
- 2. https://onlinecourses.swayam2.ac.in/cec20 ma03/preview

	Course Outcomes					
	CO-Statements	Cognitive				
CO No.	On successful completion of this course, students will be able to	Levels (K - Level)				
CO1	acquire in-depth knowledge on vital concepts in graph theory.	K1				
CO2	understand the graphs, its types and on the theory of connectivity, colorings and planarity.	K2				
CO3	apply the imbibed knowledge on the concepts to categorize graphs.	К3				
CO4	analyze and infer properties of graphs and its associated concepts.	K4				
CO5	evaluate various parameters of a graph.	K5				
CO6	construct graphs with specific properties.	K6				

					Relation	onship	Matrix				
Semester	Cours	Course code Title of the C								Hours	Credits
1	23PM	A1ES01		Electiv	e - 1: Gra	ph Theory	and its A	pplications	5	5	3
Course Outcomes	Programme Outcomes (POs) Programme Specific Outcomes (PSOs					PSOs)	Mean Score of COs				
	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	COS
CO1	2	3	3	2	3	3	2	2	2	3	2.5
CO2	3	2	2	3	2	2	3	2	2	3	2.4
CO3	2	3	2	2	2	3	3	3	2	2	2.4
CO4	2	2	3	2	2	2	2	3	3	2	2.3
CO5	3	2	2	3	2	3	2	2	2	3	2.4
CO6	3	2	3	3	2	2	3	2	2	2	2.4
	•	•				•		N	lean over	all Score	2.4 (High)

Semester	Course code	Title of the Course	Hours	Credits
1	23PMA1ES02	Elective - 2: Fuzzy Sets and Their Applications	5	3

To enable the students to understand the concept of fuzzy logic, fuzzy sets, properties of  $\alpha$ -cuts, extension principles

To enable the students to understand the generalized concepts of fuzzy complements, t-norm and t-conorm

To provide the idea of fuzzy numbers, fuzzy relations, fuzzy equivalence relations

To distinguish possibility theory and probability theory

To understand the decision-making process and apply them to real life problems

#### **UNIT I: Basics of Fuzzy Sets:**

(15 Hours)

Fuzzy sets – introduction, Basic types and Basic concepts, Additional properties of  $\alpha$ -cuts, Representation of fuzzy sets, Extension principles

#### **UNIT II: Operations on Fuzzy Sets**

**(15 Hours)** 

Type of operators on fuzzy sets and fuzzy complements, Fuzzy intersection and fuzzy unions, Combination of operations

#### **UNIT III: Fuzzy Arithmetic and Fuzzy Relations**

(15 Hours)

Fuzzy numbers, arithmetic operations on intervals, Arithmetic operations on fuzzy numbers, Fuzzy equations, fuzzy relations: Binary fuzzy relations and binary relation on a single set, Fuzzy equivalence relations

#### **UNIT IV: Possibility Theory**

(15 Hours)

Fuzzy measures - Evidence theory - Possibility theory - Fuzzy sets and Possibility theory - Possibility theory versus Probability theory

#### **UNIT V: Fuzzy Decision making**

**(15 Hours)** 

Introduction, Individual Decision Making, Multiperson decision Making, Multicriteria decision Making, Fuzzy ranking methods

Teaching Methodology	Chalk and Talk, PPT
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#### **Books for Study:**

1. Klir, G. J. & Yuan, B. (1997). Fuzzy sets and Fuzzy logic – Theory and applications. Prentice Hall India.

**Unit I:** Chapter 1 and Chapter 2: Sections 1.3, 1.4, 2.1 to 2.3

Unit II: Chapter 3: Sections 3.1 to 3.5

**Unit III:** Chapter 4 and Chapter 5: Sections 4.1, 4.3, 4.4, 5.1 to 5.5

Unit IV: Chapter 7: Sections 7.1 to 7.5 Unit V: Chapter 15: Sections 15.1 to 15.6

#### **Books for Reference**

1. Zimmermann, H. J. (1987). Fuzzy sets, decision making and expert systems. Kluwer.

2. Chen, S. J. & Hwang, C. L. (1992). Fuzzy multiple attributes decision making. Springer Verlag.

Course Outcomes						
	CO-Statements	Cognitive				
CO No.	On successful completion of this course, students will be able to	Levels (K - Level)				
CO1	acquire the knowledge of various types of fuzzy sets, $\alpha$ -cuts and its properties and extension of functions.	K1				
CO2	understand various operations (fuzzy complements, fuzzy intersections and fuzzy unions) on fuzzy sets and symbolic computations.	K2				
CO3	apply the concepts of fuzzy decision-making methods in engineering and management problems.	К3				
CO4	distinguish possibility theory and probability theory	K4				
CO5	Explain various fuzzy related concepts	K5				
CO6	Create the fuzzy relations and identify the different types of fuzzy relations and their applications numbers, divisors, modulo arithmetic, primitive roots and quadratic residues.	K6				

	Relationship Matrix										
Semester	Cours	Course code Title o				of the Co	ourse			Hours	Credits
1	23PMA	1ES02		Electiv	e - 2: Fuzz	zy Sets an	d Their A	pplications	3	5	3
Course Outcomes		Programi	ne Outco	mes (POs	)	Programme Specific Outcomes (I			mme Specific Outcomes (PSOs)		
	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	
CO1	2	2	1	2	2	3	2	2	3	3	2.2
CO2	2	1	2	1	2	2	3	3	3	2	2.1
CO3	1	2	2	3	1	2	3	3	3	2	2.2
CO4	3	2	1	2	3	2	3	3	2	1	2.2
CO5	2	3	2	3	1	3	3	2	3	3	2.5
CO6	1	2	2	3	1	2	3	3	3	2	2.2
Mean overall Score							2.2 (High)				

Semester	Course code	Title of the Course	Hours	Credits
1	23PMA1AE01	Ability Enhancement Course: Problem Solving in Advanced Mathematics	2	1

To understand the concepts in Real Analysis, Algebra and Ordinary differential equations

To recall the fundamental ideas in various interpretations of the problems

To create many examples to justify the answers

To analyze and apply the results and techniques to get solutions

To train the students in problem-solving as a preparatory to NET/SET

UNIT I (6 Hours)

Sets – open – closed – compact – connected - Sequences and series.

UNIT II (6 Hours)

Continuity – uniform continuity – differentiability – mean value theorems – Riemann integral – Uniform convergence.

UNIT III (6 Hours)

Groups – subgroups – normal subgroups – cyclic groups – quotient groups – homomorphisms – permutation groups.

UNIT IV (6 Hours)

Cayley's theorem – class equations – Sylow theorems – Rings – ideals – quotient rings – prime and maximal ideals.

UNIT V (6 Hours)

Wronskian – Existence and uniqueness of solutions of initial value problems for first order ordinary differential equations.

Teaching Methodology	Chalk and talk, Lectures, Demonstrations, PPT.
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#### **Books for Study**

1. Singh, A.P. (2017). *Info study's real analysis*. Info study Publications

**Unit I:** *Chapter 1*: 1.1, 1.24 – 1.40, *Chapter 2*: 2.1 – 2.2

**Unit II:** *Chapter 3*: 3.1 – 3.3, 3.5.3,

*Chapter 2*: 2.3, *Chapter 5*: 5.1

2. Singh, A.P. (2017). *Info study's modern algebra*. Info study Publications **Unit III:** *Chapter 1*: 1.1 – 1.2, 1.5 – 1.7, 1.10

*Chapter 2*: 2.1 – 2.4

**Unit IV:** *Chapter 2*: 2.5 – 2.7, 3.5.3,

*Chapter 3*: 3.1 – 3.8, 3.10, 3.11, 3.15.6, 3.15.7

3. Singh, A.P. (2017). Info study's differential equation. Info study Publications

**Unit V:** *Chapter 2*: 2.10, *Chapter 3*: 3.1

- 1. Rudin, W. (1976). *Principles of mathematical analysis* (3<sup>rd</sup> ed.). McGraw-Hill International Book Company.
- 2. Gallian, J. A. (2012). *Contemporary abstract algebra* (7<sup>th</sup> ed.). Katherine Tegan Books.
- 3. Coddington, E. A. (1992). *An introduction to ordinary differential equations*. Prentice-Hall of India.

	Course Outcomes						
CO No	CO-Statements	Cognitive Levels					
CO No.	On successful completion of this course, students will be able to	(K - Level)					
CO1	analyze the efficiency of a specific technique when solving a problem.	K4					
CO2	evaluate various interpretations of the problems	K5					
CO3	develop new problem-solving methodology to tackle problems in Advanced Mathematics	K6					

					Relation	onship	Matrix				
Semester	Cours	se code			Title	of the C	ourse			Hours	Credits
1	1 23PMA1AE01 Ability Enhancement Course: Problem Solving in Advanced Mathematics						2	1			
Course Outcomes	Program			me Outcomes (POs)			Programme Specific Outcomes (				Mean Score of
	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	COs
CO1	2	2	2	2	1	3	3	3	2	3	2.3
CO2	1	3	2	1	1	2	3	3	1	2	1.9
CO3	2	2	2	2	2	3	3	3	2	2	2.3
	Mean overall Score								2.2 (High)		

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PMA2CC04	Core Course - 4: Advanced Algebra	6	6

To gain deep understanding of important concepts of extension fields and roots of Polynomials, field theory and develop proficiency in their applications.

To investigate the structure and behavior of algebraic systems and classify them based on certain properties, and apply the concepts to solve various mathematical problems in diverse areas of studies.

To understand the concepts of Hermitian, unitary and normal linear transformations and their properties, simplifying their representation, and analyzing their behaviors in various mathematical contexts.

To simplify real quadratic forms and to classify various linear transformations efficiently.

To provide insights into finite fields and finite division rings.

UNIT I (18 Hours)

Extension fields - The Transcendence of e.

UNIT II (18 Hours)

Roots of Polynomials - More about roots

UNIT III (18 Hours)

Elements of Galois theory.

UNIT IV (18 Hours)

Finite fields - Wedderburn's theorem on finite division rings.

UNIT V (18 Hours)

Solvability by radicals - A theorem of Frobenius - Integral Quaternions and the Four - Square theorem.

<b>Teaching Methodology</b>	Chalk and talk, Lectures, Demonstrations, PPT.
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#### **Books for Study**

1. Herstein, I. N. (1975), *Topics in Algebra* (2nd Ed.) Wiley Eastern Limited.

**Unit I** Chapter 5: Section 5.1 and 5.2

**Unit II** Chapter5: Sections 5.3 and 5.5

**Unit III** Chapter 5: Section 5.6

**Unit IV** Chapter7: Sections7.1 and 7.2(Theorem 7.2.1 only)

Unit V Chapter5: Section 5.7 (omit Lemma 5.7.1, Lemma 5.7.2 and Theorem 5.7.1),

Chapter 7: Sections 7.3 and 7.4

- 1. Artin, M. (1991). Algebra. Prentice Hall of India.
- 2. Bhattacharya, P. B., Jain, S. K., & Nagpaul, S.R. (1997). *Basic Abstract Algebra* (2nd Ed.). Cambridge University Press.
- 3. Luther, I. S. & Passi, I. B. S. (1996). *Algebra, Vol. I-Groups; Vol. II Rings*, Narosa Publishing House.
- 4. Malik, D. S., Mordeson, J. N., & Sen, M. K. (1997). Fundamental of Abstract Algebra, McGraw-Hill.
- 5. Jacobson, N. (1980). *Basic Algebra, Vol. I & II W.H. Freeman.* Hindustan Publishing Company.

- Website and eLearning Sources

  1. http://mathforum.org

  2. http://ocw.mit.edu/ocwweb/Mathematics,

  3. http://www.opensource.org

  4. www.algebra.com

Course Outcomes						
CO No.	CO-Statements					
CO No.	On successful completion of this course, students will be able to	Levels (K- Level)				
CO1	recall basic concepts on Vector spaces, define finite extension, define the number, define Hermitian, unitary and normal transformations, define Galois groups and finite fields	K1				
CO2	classify the roots of a polynomial, summarize remainder theorem, understand the characteristics of a field, summarize Wedderburn's theorem and Frobenius theorem.	К2				
CO3	relate solve ability for Galois groups, prove e is transcendental, relate unitary linear transformation to orthonormal basis	К3				
CO4	illustrate Hermitian, unitary and normal linear transformations with examples.	<b>K4</b>				
CO5	demonstrate knowledge and understanding of fundamental concepts including extension fields, Algebraic extensions, Finite fields, Class equations and Sylow's theorem.	К5				
CO6	develop new results based on Wedderburn's theorem, Frobenius theorem and the Four-square theorem.	К6				

					Relation	ship Ma	trix				
Semester	C	ourse Co	ode		Т	itle of tl	ne Cours	e		Hours	Credits
2	23	PMA2C	C <b>04</b>	(	Core Course - 4: Advanced Algebra						6
Course	P	rogramn	ne Outco	atcomes (POs) Programme Specific Outcomes (PS				(PSOs)	Mean		
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Score of COs
CO1	3	3	3	2	1	3	2	3	2	3	2.5
CO2	2	3	3	2	2	2	3	2	1	3	2.3
CO3	3	2	3	2	2	3	2	2	2	2	2.3
CO4	3	3	2	2	2	3	3	3	2	3	2.6
CO5	2	3	3	2	1	3	3	2	2	3	2.4
CO6	2	3	3	2	1	3	3	2	2	3	2.4
		1	1		l .			I	Mean Ove	rall Score	2.42 (High

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PMA2CC05	Core Course - 5: Real Analysis - 2	5	4

To give the students a thorough knowledge of the various aspects of real line and metric spaces.

To train the students for advanced learning in pure mathematics

To give the students the knowledge of analyzing and approaching life

To train the students to apply pure mathematics to applied problems

To train the students in problem-solving as a preparatory to NET/SET

**UNIT I** (15 Hours)

Finite, Countable and Uncountable Sets - Metric Spaces - Compact Sets - Perfect Sets - Connected Sets.

**UNIT II** (15 Hours)

The Root and Ratio Tests- Power Series-Summation by Parts - Absolute Convergence - Continuous functions - Continuity and Compactness - Continuity and Connectedness-Mean Value Theorems-L 'Hospital's Rule-Taylor's Theorem

UNIT III (15 Hours)

Power Series - The Exponential and Logarithmic Functions - The Trigonometric Functions-The Algebraic Completeness of the Complex Field.

**UNIT IV** (15 Hours)

Fourier Series - Parseval's Theorem-The Gamma Function.

**UNIT V** (15 Hours)

Linear Transformations - Differentiation - The Contraction Principle - The Inverse Function Theorem.

Teaching Methodology	Chalk and Talk, PPT
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#### **Book for study**

1. Rudin, W. (1976). Principles of Mathematical Analysis, (3rd Ed.). McGraw-Hill.

Unit I Chapter 2

**Unit II** Chapter 3 (Sec: 3.33-3.46), Chapter 4 (Sec: 4.5-4.24)

Chapter 5 (Sec: 5.7-5.11, 5.13, and 5.15)

Chapter 8 (Sec: 8.1-8.8) **Unit III** Chapter 8 (Sec: 8.9-8.22) **Unit IV** Unit V Chapter 9 (Sec: 9.1-9.25)

- 1. Apostol, T.M. (1974). *Mathematical Analysis*. Addison, Wesley Publishing Company.
- 2. Goldberg, R. R. (1970). *Methods of Real Analysis*. Oxford & IBH Publishing Company.

	Course Outcomes	
CO No	CO-Statements	Cognitive
CO No.	On successful completion of this course, students will be able to	Levels (K - Level)
CO1	gain knowledge of concepts of modern analysis such as convergence, continuity, completeness and compactness in the Euclidean space and more general metric spaces.	K1
CO2	understand the properties of some special functions and the limits and how they used in convergence properties of sequence and series, continuity and derivative of real functions.	K2
CO3	identify the applications of integration, linear transformation And power series.	К3
CO4	analyze the abstract ideas and various methods in mathematical analysis and apply them to practical problems.	K4
CO5	construct mathematical proofs for basic results as associated with the Continuity and differentiability of real valued functions.	K5
CO6	evaluate problems on the concepts learned.	K6

Relationship Matrix											
Semester	Cou	rse Code			Ti	tle of the	Course			Hours	Credits
2	23PN	MA2CC05	;	(	Core Cou	rse - 5: R	eal Analy	sis - 2		5	4
Course	P	rogramm	e Outco	mes (PO	s)	Progra	mme Spe	cific Out	comes (l	PSOs)	Mean
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Scores of COs
CO1	2	2	1	1	1	2	2	2	1	1	1.5
CO2	3	2	2	1	1	3	2	2	1	1	1.8
CO3	1	1	3	3	1	2	2	3	3	1	2
CO4	2	3	2	2	1	2	2	2	2	1	1.9
CO5	2	2	2	1	1	2	1	3	2	2	1.8
CO6	2	2	1	2	2	2	3	3	2	2	2.1
Mean Overall Score										1.85 (Medium)	

	Semester	Course Code	Title of the Course	Hours/Week	Credits
Ī	2	23PMA2CC06	Core Course - 6: Complex Analysis	6	5

To develop Knowledge and understand the fundamental concepts of Analytic Functions

To enhance problem-solving skills with line integrals

To enable the use of singularities

To enrich a proper understanding of definite integrals

To develop Knowledge about power series expansion

UNIT I (18 Hours)

Concept of Analytic Function, Limits and Continuity - Analytic Functions - Polynomials-Rational Functions- Power series - Abel's Limit Theorem.

UNIT II (18 Hours)

Complex Integration - Fundamental Theorems - Line Integrals - Rectifiable arcs - Line integrals as Functions of Arcs - Cauchy's Theorem for a Rectangle - Cauchy's Theorem in a Disk.

UNIT III (18 Hours)

Cauchy's Integral Formula - The index of appoint with respect to a closed curve - The integral formula- Higher Derivatives - Removable Singularities Taylor's Theorem.

UNIT IV (18 Hours)

The Maximum principle - The Calculus of Residues - The Residue theorem - The Argument principle-Evaluation of Definite Integrals.

UNIT V (18 Hours)

Harmonic functions, Power Series expansion - Poisson's Formula - Schwarz's Theorem - Weier strass's Theorem - The Taylor series -The Laurent series

Teaching Methodology	Chalk and Talk, PPT
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#### **Book for Study**

1. Ahlfors, L.V. (2013). Complex Analysis: An Introduction to the Theory of Analytic Functions of One Complex Variable, (3rd Ed.). Mac Millan Publishers.

**UNIT-I** Chapter 2 (sec: 1.1-1.4,2.4 & 2.5 Pages 21-33, 38-42)

**UNIT-II** *Chapter 4 (sec1.1-1.5 Pages 101-114)* 

**UNIT-III** *Chapter 4 (sec2.1-2.3, 3.1 Pages 114-126)* 

**UNIT-IV** Chapter 4 (sec3.4,5.1-5.3 Pages 133-137,148-161)

**UNIT-V** Chapter 4 (sec 6.3 & 6.4) Chapter 5 (sec 1.1-1.3 Pages 166-172, 175-186)

- 1. Conway, J.B. (1978). *Function of one Complex Variable*. (2nd Ed.). Springer Graduate Texts in Mathematics.
- 2. Ponnusamy, S. (2005). *Foundations of Complex Analysis*, (2nd Ed.). Narosa Publishing House.

	Course Outcomes					
CO No.	CO-Statements					
	On successful completion of this course, students will be able to	Levels (K - Level)				
CO1	acquire knowledge on fundamental concepts of Analyticity, Complex integration and Harmonic Functions.	K1				
CO2	understand the behavior of Analytic Functions, Taylor's and Laurent's Series expansions.	K2				
CO3	apply C-R equations, Residue Theorem in solving problems involving complex function theory.	К3				
CO4	demonstrate a good understanding of Mathematical reasoning through Cauchy's Theorem.	K4				
CO5	evaluate integrals, region of convergence and contour integrals.	K5				
CO6	analyze sequence and series of analytic functions, types of convergence, apply the concept and consequences of harmonic function, represent functions as Taylor and Laurent series	К6				

				Rel	ationship	Matrix					
Semester	Co	urse Cod	e	Title of the Course  Core Course - 6: Complex Analysis							Credits
2	23P	MA2CC(	)6								5
Course		Progran	nme Outc	comes (PO) Progr			amme S <sub>l</sub>	ecific O	utcomes	(PSOs)	Mean
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Scores of COs
CO1	3	2	1	2	2	3	2	3	2	3	2.3
CO2	3	2	2	2	2	3	2	2	2	2	2.2
CO3	3	2	2	2	2	2	2	3	2	3	2.3
CO4	2	2	2	2	2	2	2	2	2	3	2.1
CO5	2	2	2	2	2	2	2	3	2	3	2.2
CO6	2	2	2	2	2	2	2	3	2	2	2.2
Mean Overall Score										2.2 (High)	

Semester	<b>Course Code</b>	Title of the Course	Hours/Week	Credits
2	23PMA2SP01	<b>Self-paced Learning:</b> History of Mathematics	-	2

Course Outcomes
Knowledge on the History of Decimals and Limits
Acquaintance with the development of Algebra
Familiarity of Invention of Differential Calculus
The lives of Eratosthenes and Dirichlet
The lives of Henri Poincare and Emmy Noether

#### **UNIT I**

The Ancient Greeks - Pythagoras- Introduction to Pythagorean Ideas-Euclid - Introduction to Euclid - Archimedes - The Genius of Archimedes-Zeno's Paradox and the Concept of Limit- The Context of the Paradox? - Consideration of the Paradoxes - Decimal Notation and Limits - Infinite Sums and Limits-Finite Geometric Series

#### **UNIT II**

The Arabs and the Development of Algebra - The Development of Algebra Al-Khwarizmi and the Basics of Algebra- The Life of Al- Khwarizmi- Omar Khay yam and the Resolution of the Cubic-Cardano, Abel, Galois, and the Solving of Equations - A Particular Equation - The General Case - The Brief and Tragic Lives of Abel and Galois - The Work of Abel and Galois in Context- Rene Descartes and the Idea of Coordinates- Introductory Remarks-The Life of Rene Descartes - The Real Number Line- The Cartesian Plane - Coordinates in Three- Dimensional Space.

#### UNIT III

The Invention of Differential Calculus - The Life of Fermat - Fermat's Method-Fermat's Lemma and Maximum/Minimum Problems - Complex Numbers and Polynomials-Progenitors of the Complex Number System - Cardano - Argand - Cauchy - Riemann - Complex Number Basics - The Fundamental Theorem of Algebra - Finding the Roots of a Polynomial- Cauchy and the Foundations of Analysis - Why Do We Need the Real Numbers?

#### UNIT IV

The Prime Numbers - The Sieve of Eratosthenes- The Infinitude of the Primes -Dirichletand How to Count - The Life of Dirichlet - The Pigeonhole Principle - Riemann and the Geometry of Surfaces-Introduction- Georg Cantor and the Orders of Infinity-Introductory Remarks- An Uncountable Set-Countable and Uncountable-The Existence of Transcendental Numbers.

#### IINIT V

Henri Poincare, Child Prodigy - Introductory Remarks - Emmy Noether and Algebra - The Life of Emmy Noether- Emmy Noether and Abstract Algebra: Groups-Emmy Noether and Abstract Algebra: Rings -The Idea of an Ideal-Cryptography- What is Cryptography?

Teaching Methodology	JOSTEL
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#### **Books for Study**

1. Krantz, S.G. (2010). *An Episodic History of Mathematics*. The Mathematical Association of America.

Unit I Sec: 1.1,1.1.1, 1.2, 1.2.1, 1.3,1.3.1, 2.1, 2.3, 2.4-2.6.

Unit II Sec: 4.2,4.2.1, 4.2.2, 4.2.4, 5.6,5.7, 5.7.1, 5.7.2, 5.8.1, 5.9, 6.0-6.3, 6.5.

Unit III Sec: 7.1,7.2, 7.4, 8.2, 8.2.1-8.2.5,8.3, 8.4, 8.5, 10.1,10.2.

Unit IV Sec: 11.1,11.2, 12.1, 12.2,13.0,14.1, 14.2.1, 14.2.2,14.3.

Unit V Sec: 16.1,18.1, 18.2,18.3, 18.3.1, 20.3.

#### **Books for Reference**

1. Boyer, C.B., Merzbach, U. (2011). History of Mathematics, (3rd Ed.). John Wiley & Sons.

# 2. Bell, E. T. (1986). Men of Mathematics. Simon & Schuster.

	Course Outcomes	
CO No.	CO-Statements	Cognitive Levels
CO No.	On successful completion of this course, students will be able to	(K - Level)
CO1	acquire knowledge on the history of mathematics	K1
CO2	understand the inter relations among the various branches of mathematics.	K2
CO3	predict the dynamic nature of mathematics including recent development in pure and applied mathematics.	К3
CO4	identify various proof techniques used in theorems.	K4
CO5	assess creative and flexible thinking by studying historical evidences that there are different ways to view a mathematical concept.	K5
CO6	construct abstract characterization of ideas from known examples.	<b>K</b> 6

Relationship Matrix											
Semester	Co	urse Coo	de			Title of th	ne Course	:		Hours	Credits
2	23P	PMA2SP	01	Self-	paced L	earning:	History of	Mathema	itics	-	2
Course	Pı	rogramn	ne Outco	omes (PC	Os)	Prog	ramme S	pecific O	itcomes (	PSOs)	Mean
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Score of COs
CO1	1	2	3	1	2	2	3	3	2	3	2.2
CO2	1	2	3	1	2	2	3	3	2	3	2.2
CO3	2	3	3	1	1	3	1	3	2	3	2.2
CO4	2	3	2	1	2	2	3	3	1	3	2.2
CO5	2	2	2	1	2	2	3	3	3	3	2.3
CO6	2	2	3	1	2	2	3	2	1	3	2.1
Mean Overall Score										2.2 (High)	

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PMA2ES03A	Elective - 3: Algebraic Number Theory	5	4

To understand the basic concepts such as divisibility, primes, congruences and solutions in congruences

To know some techniques of abstract algebra to study integers

To highlight the knowledge on Quadratic residues

To highlight some of the Applications of the Theory of Numbers.

To get the more knowledge on Diophantine Equations

UNIT I (15 Hours)

Introduction - Divisibility - Primes - The Binomial Theorem - Congruences Euler's totient - Fermat's, Euler's and Wilson's Theorems - Solutions of Congruences - The Chinese Remainder theorem.

UNIT II (15 Hours)

Prime power Moduli - Primitive roots and Power Residues - Number theory from an Algebraic Viewpoint- Groups, rings and fields.

UNIT III (15 Hours)

Quadratic Residues - Quadratic Reciprocity - The Jacobi Symbol - Binary Quadratic Forms-Equivalence and Reduction of Binary Quadratic Forms-sum of two squares.

UNIT IV (15 Hours)

Greatest integer Function - Arithmetic Functions - The Mobius Inversion Formula Recurrence Functions-Combinatorial number theory

UNIT V (15 Hours)

Diophantine Equations - The equation ax + by = c - Simultaneous Linear Diophantine Equations-Pythagorean Triangles- Assorted examples

<b>Teaching Methodology</b>	Chalk and Talk, PPT, Video Lecture
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#### **Book for Study**

1. Niven, I., Zuckerman, H.S., & Montgomery, H.L. (2004). *An Introduction to the Theory of Numbers*, (5th Ed.). John Wiley & Sons Inc.

**Unit- I** Chapter 1 and Chapter 2: Sections 2.1 to 2.3

Unit- II Chapter 2: Sections 2.6 to 2.11

**Unit- III** *Chapter 3: Sections 3.1 to 3.6* 

Unit- IV Chapter 4

Unit- V Chapter 5: Sections 5.1 to 5.4

- 1. Jones, G.A., & Jones, M. J. (2005). Elementary Number Theory. Springer Verlag,
- 2. Burton, D.M. (2007). Elementary Number Theory, (6th Ed.). McGraw-Hill.
- 3. Andrews, G. (1971). Theory of Numbers. Saunders.
- 4. William, J. (1977). Fundamentals of Number Theory, Levegue, Addison-Wesley.

Course Outcomes							
CO No.	CO-Statements						
	On successful completion of this course, students will be able to	Levels (K - Level)					
CO1	have knowledge of divisibility, prime numbers, congruences, quadratic reciprocity and Diophantine equations.	K1					
CO2	understand the concept of number theory toper form numerical and symbolic computations.	K2					
CO3	solve problems and give short proofs associated with prime numbers, divisors, modulo arithmetic, primitive Roots and quadratic residues.	К3					
CO4	analyze the theory of congruences, Power Residues, The Jacobi Symbol, The Mobius Inversion Formula and linear Diophantine equations.	K4					
CO5	evaluate and produce rigorous arguments centered on the material of number theory, most notably in the use of mathematical Induction and/or the Well Ordering Principal in the proof of theorems.	К5					
CO6	construct and produce rigorous arguments centered on the material of number theory in the proof of theorems.	К6					

Relationship Matrix											
Semester	Cou	ırse Cod	e		T	itle of the	Course			Hours	Credits
2	23PN	1A2ES03	ВА	F	Elective - 3	: Algebrai	c Number	Theory		5	4
Course	F	rogram	me Outc	omes (P	Os)	Progr	amme Spe	ecific Out	comes (P	SOs)	Mean Scores
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	of COs
CO1	2	2	1	2	2	3	2	2	3	3	2.2
CO2	2	1	2	1	2	2	3	3	3	2	2.1
CO3	1	2	2	3	1	2	3	3	3	2	2.2
CO4	3	2	1	2	3	2	3	3	2	1	2.2
CO5	2	3	2	3	1	3	3	2	3	3	2.5
CO6	3	2	1	2	3	2	3	3	2	1	2.2
	Mean Overall Score										

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PMA2ES03B	Elective - 3: Optimization Techniques	5	4

To explain the concepts and to simultaneously develop an understanding of problem Solving methods

To study the basic components of an optimization problem.

Formulation of design problems as mathematical programming problems

To highlight some of the Applications of the optimization techniques

To impart Optimization Techniques

UNIT I (15 Hours)

Optimization of functional - Gateaux and Fréchet Differentials - Fréchet derivatives - Extrema-Euler - Lagrange Equations- Problems with variable end points.

UNIT II (15 Hours)

Convex and concave functionals - Conjugate convex, concave functional - Dual optimization problems- Min - Max theorem of game theory.

UNIT III (15 Hours)

Lagrange multiplier theorem- Inverse function theorem- Equality and Inequality constraints

- Kuhn- Tucker theorem.

UNIT IV (15 Hours)

Methods of solving equations - Successive approximation - Newton's method - Descent methods-Steepest descent.

UNIT V (15 Hours)

Conjugate gradient method - Methods for solving constrained problems - Projection method - The Primal - Dual method - Penalty Functions.

Teaching Methodology	Chalk and Talk, PPT, Video Lecture
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#### **Book for Study**

1. Luenberger, D.G. (1997). *Optimization by Vector Space Methods*. Wiley Professional Paperback series.

**Unit- I** (Sec7.1-7.6 Pages 169-184)

**Unit- II** (Sec 7.8, 7.10-7.13 Pages 190, 191,195-208)

Unit-III (Sec9.1-9.4 Pages 239-253)

**Unit-IV** (Sec 10.1-10.5 Pages 271-289)

**Unit- V** (Sec10.8-10.11 Pages 294-307)

- 1. Dorney, C.N. (1986). A Vector Space Approach to Models and Optimization. Robert Krieger Publishing Co.
- 2. Mohan, C. & Deep, K. (2010). *Optimization Techniques*. New Age International.
- 3. Hamley, A. & Taha. (2011). Operations Research: An introduction, (19th Ed.). Prentice Hall.

Course Outcomes								
CO No.	CO-Statements	Cognitive						
	On successful completion of this course, students will be able to	Levels (K - Level)						
CO1	relate the concepts of theory of optimization while solving problems.	K1						
CO2	understand the theory behind optimization techniques.	K2						
CO3	apply suitable theory in the optimal problem.	К3						
CO4	compare the uses of different theories and methods available.	K4						
CO5	evaluate the optimal solution for the given function.	К5						
CO6	create some new techniques for optimization	K6						

Relationship Matrix													
Semester Course Code			le	Title of the Course							Hours	Credits	
2	23PN	MA2ES0	3B	Elective - 3: Optimization Techniques								4	
Course	Programme Outcomes (POs)					Programme Specific Outcomes (PSOs)						Mean	
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	.	ores of COs	
CO1	3	2	2	1	2	3	2	2	2	2		2.1	
CO2	2	3	1	2	2	3	2	3	2	2		2.2	
CO3	3	3	2	2	2	3	2	3	1	2		2.3	
CO4	2	2	3	3	2	2	1	2	2	2		2.1	
CO5	3	2	2	2	1	3	2	3	2	3		2.3	
CO6	3	3	2	2	2	3	2	3	1	2		2.3	
Mean Overall Score											2.2	(High)	

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PSS2SE01	Skill Enhancement Course: Soft Skills	4	3

Course Objectives
To provide a focused training on soft skills for students in colleges for better job

To communicate effectively and professionally

To help the students take active part in group dynamics

To familiarize students with numeracy skills for quick problem solving

To make the students appraise themselves and assess others

#### **Unit I: Effective Communication & Professional Communication**

**(12 Hours)** 

prospects

Definition of communication, Barriers of Communication, Non-verbal Communication; Effective Communication - Conversation Techniques, Good manners and Etiquettes; Speech Preparations & Presentations; Professional Communication.

#### **Unit II: Resume Writing & Interview Skills**

(12 Hours)

Resume Writing: What is a résumé? Types of résumés, - Chronological, Functional and Mixed Resume, Purpose and Structure of a Resume, Model Resume.

Interview Skills: Types of Interviews, Preparation for an interview, Attire, Body Language, Common interview questions, Mock interviews & Practicum

#### **Unit III: Group Discussion & Personal effectiveness**

(12 Hours)

Basics of Group Discussion, Parameters of GD, Topics for Practice, Mock GD & Practicum & Team Building.

Personal Effectiveness: Self Discovery; Goal Setting with questionnaires & Exercises

#### **Unit IV: Numerical Ability**

(12 Hours)

Introducing concepts Average, Percentage; Profit and Loss, Simple Interest, Compound Interest; Time and Work, Pipes and Cisterns.

#### Unit V: Test of Reasoning

(12 Hours)

Introducing Verbal Reasoning: Series Completion, Analogy; Data Sufficiency, Assertion and Reasoning; and Logical Deduction. Non-Verbal Reasoning: Series; and Classification

<b>Teaching Methodology</b>	Chalk and talk, Lectures, Demonstrations, PPT.
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#### **Book for study**

1. Melchias G., Balaiah, J. & Joy, J. L. (Eds). (2018). Winner in the Making: A Primer on soft Skills. Trichy, India: St. Joseph's College.

- 1. Aggarwal, R. S. (2010). A Modern Approach to Verbal and Non-Verbal Reasoning. S. Chand.
- 2. Covey, S. (2004). 7 Habits of Highly effective people. Free Press.
- 3. Gerard, E. (1994). The Skilled Helper (5th Ed.). Brooks/Cole.
- 4. Khera, S. (2003). You Can Win. Macmillan Books.
- 5. Murphy, R. (1998). Essential English Grammar, (2nd Ed.). Cambridge University Press.
- 6. Sankaran, K., & Kumar, M. (2010). *Group Discussion and Public Speaking* (5th Ed.). M.I. Publications.
- 7. Trishna, K. S. (2012). How to do well in GDs & Interviews? (3rd Ed.). Pearson Education.
- 8. Yate, M. (2005). Hiring the Best: A Manager's Guide to Effective Interviewing and Recruiting

	Course Outcomes								
	CO-Statements	Cognitive							
CO No.	On successful completion of this course, students will be able to	Levels (K - Level)							
CO1	recall various soft skill sets	K1							
CO2	understand personal effectiveness in any managerial positions	K2							
CO3	apply verbal and non-verbal reasoning skills to solve problems	К3							
CO4	differentiate problems at work and home; and design solutions to maintain work-life balance	K4							
CO5	assess growth and sustainability and infuse creativity in employment that increases professional productivity	K5							
CO6	construct plans and strategies to work for better human society	K6							

Relationship Matrix											
Semester	Semester Course Code					itle of the	Course		Н	ours	Credits
2	23	3PSS2SE	201	Sk	cill Enha	ncement (	Course: So	ft Skills		4	3
Course	P	rogramn	ne Outco	omes (POs) Programme Specific Outcomes (P							
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Scores of COs
CO1	3	3	3	3	2	3	2	3	2	3	2.7
CO2	3	3	3	2	3	3	3	3	3	3	2.9
CO3	3	2	2	3	3	3	3	3	3	3	2.8
CO4	3	3	2	2	3	3	3	3	3	3	2.8
CO5	3	3	3	2	2	3	3	3	3	3	2.8
CO6	3	3	3	2	2	3	3	3	3	3	2.8
Mean Overall Score											2.8 (High)

Semester	Course Code	Title of the Course	Hours/Week	Credits
2	23PMA2EG01A	General Elective - 1: (WS)  Mathematical Foundations for Computer	4	3
		Applications		

To understand fundamental concepts of mathematical logic and numerical analysis

To study the basic properties functions and relations

To develop analytical skills through the study group theory

To understand different techniques in numerical computation.

To apply numerical techniques and solve problems in roots of equation and integration

UNIT I (12 Hours)

Relations - Equivalence Relation - Functions and Operators - One-to-one, Onto Functions - Special Types of Functions - Invertible Functions - Composition of Function.

UNIT II (12 Hours)

Binary Operations - Special type of binary operations, Groups - Integral powers of an elements of a group - abelian groups.

UNIT III (12 Hours)

Lattices - Some Properties of Lattices - New Lattices - Lattice Homomorphisms - Product Lattices of Two Lattices - Modular and Distributive Lattices-Boolean Algebra.

UNIT IV (12 Hours)

Iterative Methods: Birge - Vieta - Graeffe's Root squaring methods - System of linear algebraic equations: Gauss Elimination, Jacobi iteration method - Gauss-Seidel iteration method

UNIT V (12 Hours)

Interpolation: Lagrange interpolation - Newton's Forward Difference Interpolation - Newton's Backward Difference Interpolation - Trapezoidal Rule - Simpson Rule - Romberg integration.

<b>Teaching Methodology</b>	Chalk and talk, Lectures, Problem Solving, PPT.
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#### **Books for Study**

1. Venkataraman, M.K., Sridharan, N., & Chandrasekaran, N. (2006) *Discrete Mathematics*, The National Publishing Company.

Unit-I Chapter II (Sec 2, 5), Chapter III (Sec 1, 2, 3, 4, 5).

**Unit-II** Chapter VII (Sec 1,7)

**Unit-III** *Chapter X (Sec 1,2,3,4,5) (Only Definitions and examples in Sec 4 & Sec 5)* 

2. Jain, M.K., Iyengar, S.R.K., & Jain R.K. (2003.) *Numerical Methods for Scientific and Engineering Computation*, (4th Ed.). New Age International (P) Limited.

**Unit-IV** Chapter 2 (Sec 2.9,), Chapter 3 (Sec 3.2, 3.4).

**Unit-V** Chapter 4 (Sec 4.2, 4.4), Chapter 5 (Sec 5.9, 5.10)

- 1. Tremblay, J.P., & Manohar, R. (1987). Discrete Mathematical Structures with Applications to Computer Sciences. McGraw-Hill.
- 2. Sastry, S.S. (2009). *Introductory Methods of Numerical Analysis*, (4th Ed.). PHI Learning Private Limited,
- 3. Kandasamy, P., Thilagavathy, K., & Gunavathi, K. (2008). *Numerical Methods*. S. Chand & Company Ltd

Course Outcomes							
CON	CO-Statements						
CO No.	On successful completion of this course, students will be able to	Levels (K - Level)					
CO1	acquire knowledge of relations, functions, lattices and numerical methods	K1					
CO2	understand the types of functions, groups and numerical techniques	K2					
CO3	apply composition of functions, the concept of group theory and numerical formulae	К3					
CO4	analyze various types of function, concept of Boolean algebra numerical methods to find solutions of linear equations and system of equations using different methods	K4					
CO5	justify relations and functions, properties of groups and homomorphism of lattices.	K5					
CO6	relate solutions of system of linear equations and numerical integration	K6					

	Relationship Matrix										
Semester	Cours	e Code			Hours	Credits					
2	23PMA	2EG01A	Ma	General Elective - 1:  Mathematical Foundations for Computer Applications						4	3
Course	F	rogramm	e Outcon	nes (POs	)	Progra	ımme Sp	ecific Out	tcomes (l	PSOs)	Mean
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Score of COs
CO1	3	3	3	2	1	3	2	3	2	3	2.5
CO2	2	3	3	2	2	2	3	2	1	3	2.3
CO3	3	2	3	2	2	3	2	2	2	2	2.3
CO4	3	3	2	2	2	3	2	3	2	2	2.4
CO5	2	3	3	2	1	3	3	2	2	3	2.4
CO6	2	3	3	2	1	2	3	2	2	2	2.2
Mean Overall Score										2.35 (High)	

Semo	ester	Course Code	Title of the Course	Hours/Week	Credits
			General Elective - 1:(WS)		
2	2	<b>23PMA2EG01B</b>	Mathematical Foundations for Computer	4	3
			Science		

Course Objectives
To understand fundamental concepts of mathematical logic and numerical analysis
To study the basic properties functions and relations
To develop analytical skills through the study of truth table and tautology
To understand the relationship between functions and lattices

UNIT I (12 Hours)

To apply numerical techniques and solve problems in roots of equation and integration

Relations - Equivalence Relation - Functions and Operators - One-to-one, Onto Functions - Special Types of Functions-Invertible Functions- Composition of Function- Mathematical Induction.

UNIT II (12 Hours)

Logic: Introduction - TF - Statements - Connectives - Conjunction - Disjunction - Negation - Conditional Statements - Biconditional Statements - The Truth Table of a Formula - Tautology.

UNIT III (12 Hours)

Lattices - Some Properties of Lattices - New Lattices - Lattice Homomorphisms - Product Lattices of Two Lattices - Modular and Distributive Lattices-Boolean Algebra.

UNIT IV (12 Hours)

Iterative Methods: Birge-Vieta - Graeffe's Root Squaring Methods - System of linear algebraic equations: Gauss Elimination, Jacobi iteration method-Gauss-Seidel iteration method

UNITY (12 Hours)

Interpolation: Lagrange Interpolation - Newton's Forward Difference Interpolation - Newton's Backward Difference Interpolation-Trapezoidal Rule-Simpson Rule-Romberg integration.

Teaching Methodology	Chalk and talk, Lectures, Problem Solving, PPT.
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#### **Books for Study**

1. Venkataraman, M.K., Sridharan, N., & Chandrasekaran, N. (2006). *Discrete Mathematics*. The National Publishing Company.

**Unit-I** Chapter II (Sec 2, 5), Chapter III (Sec 1, 2, 3, 4, 5), Chapter IV (Sec 2, Theorems are excluded).

**Unit-II** *Chapter IX* (Sec 1, 2, 3,6, 7)

**Unit-III** *Chapter X (Sec 1,2,3,4,5) (Only Definitions and examples in Sec 4 & Sec 5)* 

2. Jain, M.K., Iyengar, S.R.K. & Jain R.K. (2003.) *Numerical Methods for Scientific and Engineering Computation*, (4th Ed.). New Age International (P) Limited.

**Unit-IV***Chapter2* (Sec 2.9,), Chapter 3(Sec 3.2, 3.4).

**Unit-V***Chapter4* (Sec 4.2,4.4), Chapter5(Sec 5.9,5.10)

- 1. Tremblay, J.P. & Manohar, R (1987). Discrete Mathematical Structures with Applications to Computer Sciences, McGraw-HillInternational.
- 2. Sastry, S.S. (2009). *Introductory Methods of Numerical Analysis*, (4th Ed.). PHI Learning Private Limited.
- 3. Kandasamy, P., Thilagavathy, K., & Gunavathi, K. (2008). *Numerical Methods*, S. Chand & Company Ltd.

Course Outcomes							
CON	CO-Statements						
CO No.	On successful completion of this course, students will be able to						
CO1	acquire knowledge of relations, functions, mathematical logic, lattices and numerical methods	K1					
CO2	understand the types of functions, conditional statements and numerical techniques	K2					
CO3	apply mathematical induction, composition of functions and numerical formulae	К3					
CO4	analyze various types of function, statements using truth tables, Boolean algebra numerical methods to find solutions of linear equations and system of equations using different methods	K4					
CO5	justify relations and functions, to construct mathematical arguments using logical connectives and quantifiers, lattices.	К5					
CO6	Relate solutions of system of linear equations and numerical integration	K6					

					Relati	onship	Matrix				
Semester	Co	Course Code Title of the Course					Hours	Credits			
2	2 23PMA2EG01B				ematical	4					
Course	P	rogramn	ne Outc	omes (P	Os)	F	rogramm	e Specific	Outcome	(PSOs)	Mean
Outcomes	PO1	PO2	PO3	PO4	PO5	PSO1	PSO2	PSO3	PSO4	PSO5	Score of COs
CO1	3	3	3	2	1	3	2	3	2	3	2.5
CO2	2	3	3	2	2	2	3	2	1	3	2.3
CO3	3	2	3	2	2	3	2	2	2	2	2.3
CO4	3	3	2	2	2	3	2	3	2	2	2.4
CO5	2	3	3	2	1	3	3	2	2	3	2.4
CO6	2	3	3	2	1	2	3	2	2	2	2.2
Mean Overall Score									2.35 (High)		